

GRMHD Simulations of Binary Black Holes in magnetized disks

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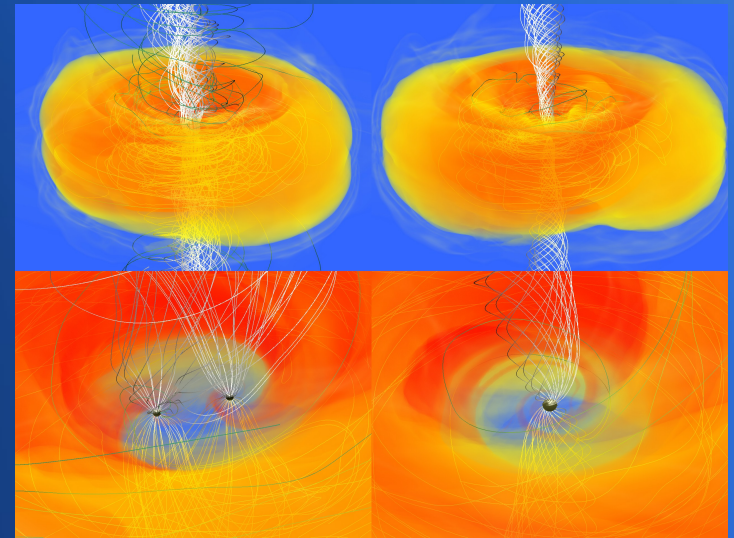


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Astro Coffee, ITP/FIAS Frankfurt, Dec 16th 2014

Outline

- Astrophysical context & Motivation
- BHBH+disks modeling
- Results, highlights
- Summary & Outlook



Galaxies merge!

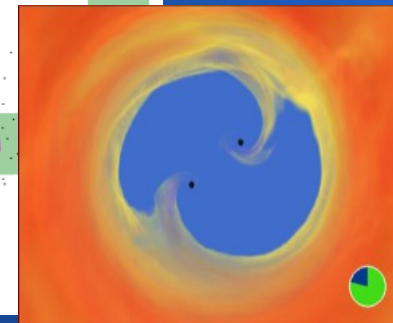
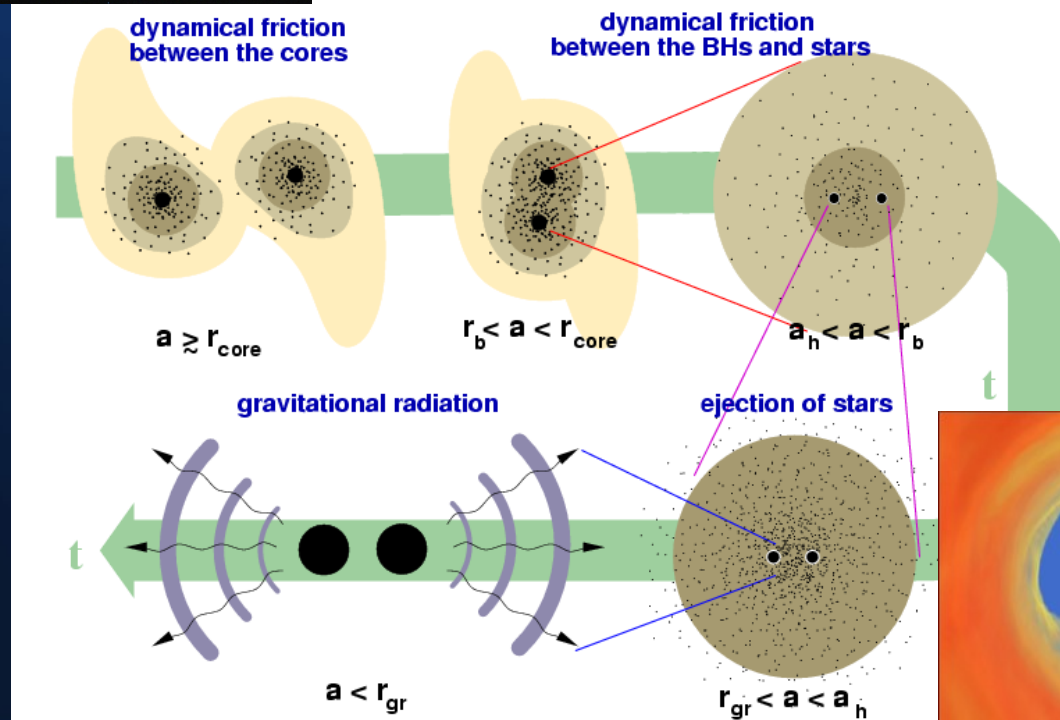


Formation of SMBH binaries



Benson 2013

MERGING OF BHs DUE TO



Farris et al 2011

Astrophysical evidence

- SMBHs grow through accretion & merger
- SMBHs accrete & shine throughout cosmic evolution
→ **SMBH merger with EM counterpart**

Observational facilities:

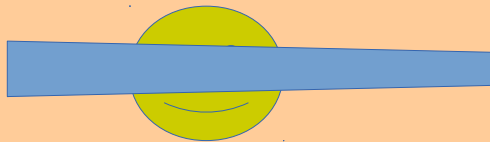
- GWs: Pulsar Timing Arrays ~2017, eLISA 2032+
- EM transients: e.g. PanStarrs, WFIRST, LSST

EM counterparts

- BHBH in vacuum: well understood system
- Now: BHBH in (magnetized) gaseous environments
- Goal: Identify EM counterpart
- Precursor (periodicities, jets, fainting, ...)
- Afterglow (merger aftermath, rebrightening, ...)
 - **Need source modeling! Know what to look for!**

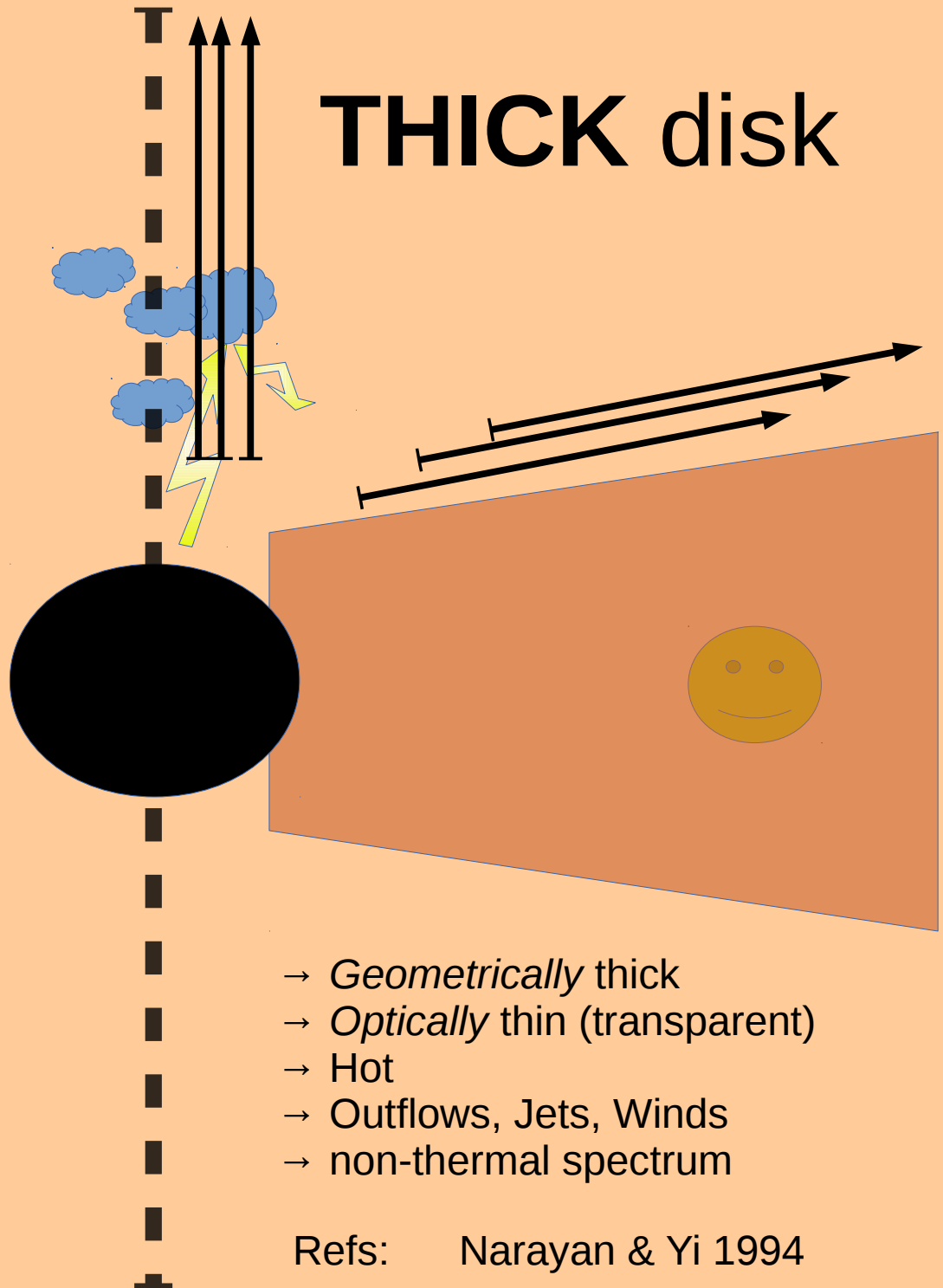
thin disk

THICK disk



- Geometrically thin
- Optically thick (opaque)
- Cold
- Truncated near BH?
- thermal spectrum

Refs: Shakura & Sunyaev 1973
Novikov & Thorne 1974

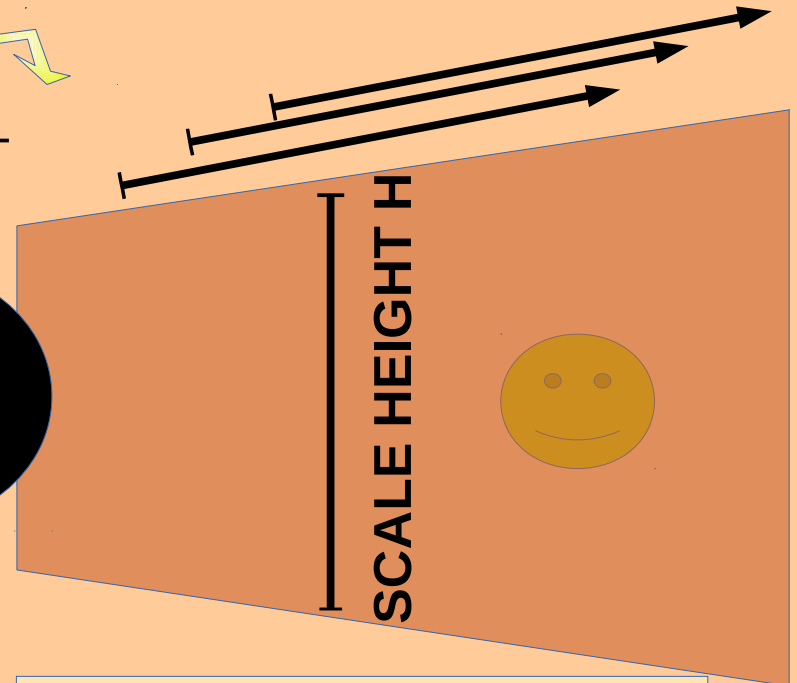
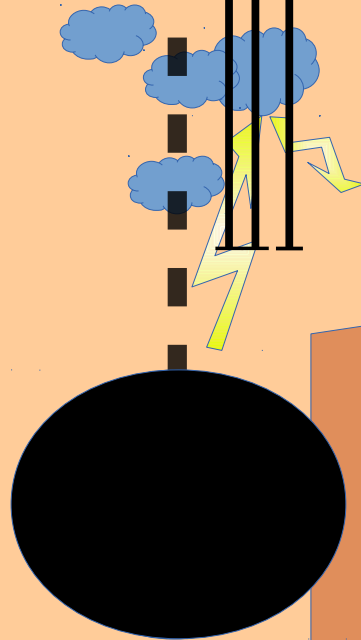
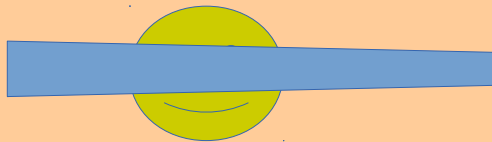


- Geometrically thick
- Optically thin (transparent)
- Hot
- Outflows, Jets, Winds
- non-thermal spectrum

Refs: Narayan & Yi 1994

thin disk

THICK disk



Gravitational potential energy

Kinetic energy

Heat

Outgoing
Radiation

Into the BH

Gravitational potential energy

Kinetic energy

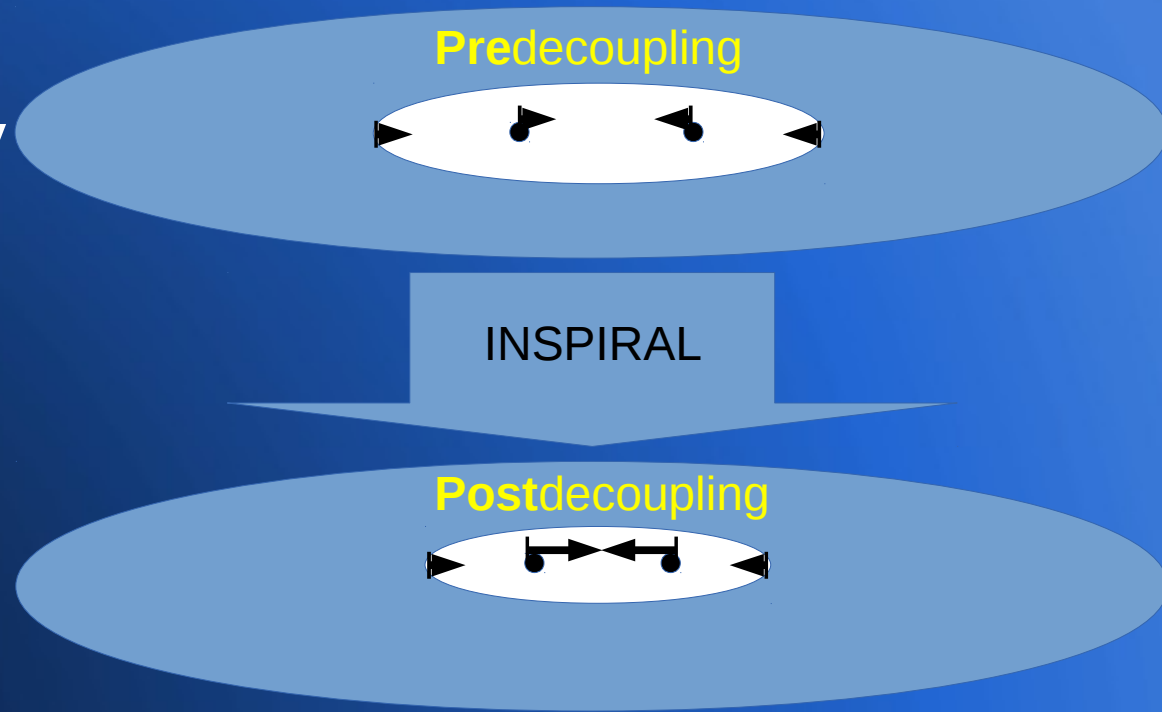
Heat

Outgoing
Radiation

Into the BH

Binary-disk decoupling

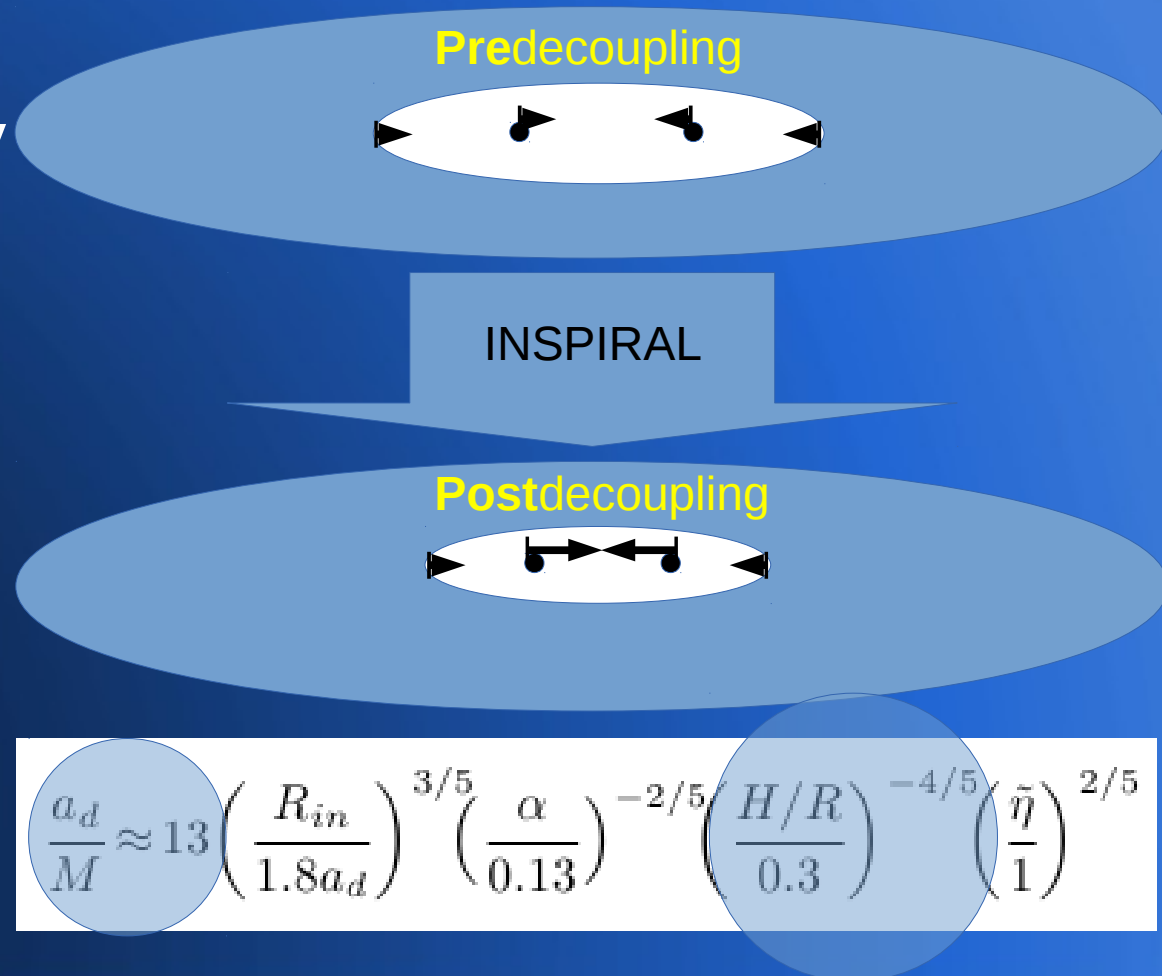
- Disc dynamics determined by interplay between viscous and binary tidal torque
- Equate disk response ($\rightarrow$ viscous) time scale with inspiral rate ($\rightarrow$ GW time scale)
- solve for separation $\rightarrow$ decoupling radius



$$\frac{a_d}{M} \approx 13 \left(\frac{R_{in}}{1.8a_d} \right)^{3/5} \left(\frac{\alpha}{0.13} \right)^{-2/5} \left(\frac{H/R}{0.3} \right)^{-4/5} \left(\frac{\tilde{\eta}}{1} \right)^{2/5}$$

Binary-disk decoupling

- Disc dynamics determined by interplay between viscous and binary tidal torque
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Magneto-rotational instability (MRI)

- disk embedded in a weak magnetic field is

stable to the MRI

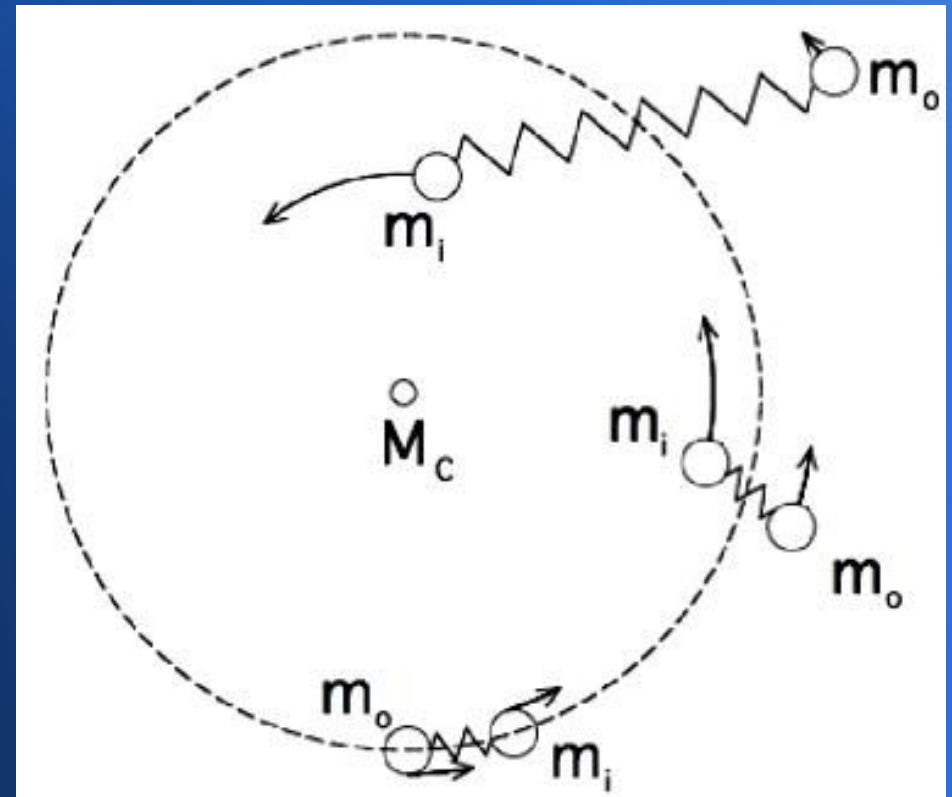
if and only if:

$$\frac{d\Omega^2}{dR} \geq 0$$

→ non-linear outcome is

MHD turbulence

- On average the turbulence acts like an **effective source of viscosity**
- Viscous torques redistribute angular momentum
→ causes **accretion**



Length and time scales: Computational Challenge

Length scales	Time scales
Resolve horizons $\Delta r \sim 10^{-2} M$	Time step $dt_{CFL} \sim 10^{-2} M$
MRI wavelength $\lambda_{MRI} \sim 10^{-1} M$	$r_g/c = M$
Horizon $r_{AH} \sim r_g = M$	$T_{Kepler}^{binary} \sim 2 \cdot 10^2 M$
binary separation $a \sim 10 M$	$T_{Kepler}^{disk} \& \omega_{MRI}^{-1} \lesssim 10^3 M$
disk inner edge $r_{in} \sim 20 M$	$t_{GW} \sim 10^3 M$
disk outer edge $r_{out} \sim 200 M$	(near ρ_{max} :) $t_{vis} \sim 10^4 M$

→ Adaptive-Mesh-Refinement (AMR)

Previous numerical work (*very* abbreviated, see papers)

Hydro ($B=0$):

Newtonian (SPH): Artymowicz & Lubow 1994, Cuadra et al 2008, Roedig et al 2011, 2012

MacFadyen et al 2008

GR: Farris et al 2011, Bode et al, Bogdanovic et al

Force-free (all in GR):

Palenzuela et al 2010

Moesta et al 2010, Alic et al 2012

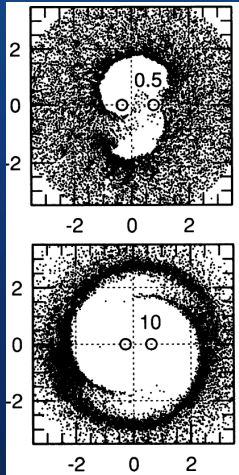
MHD:

Shi 2011 (Newtonian)

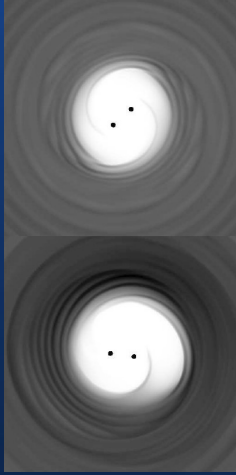
Noble et al 2012 (Post-Newtonian)

Farris et al 2012, Gold et al 2013, 2014 (GR)

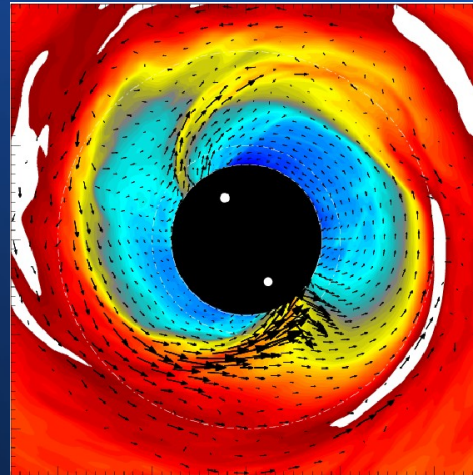
Modeling of circumbinary disks



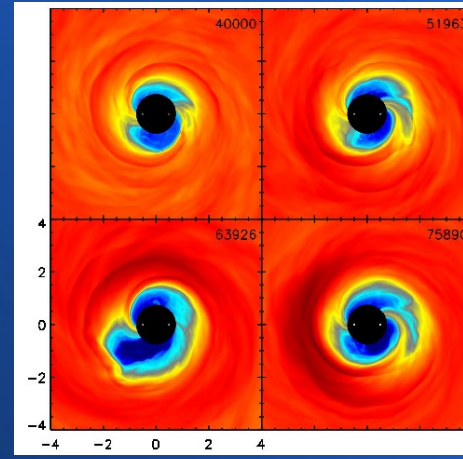
Artymowicz
et al 1994



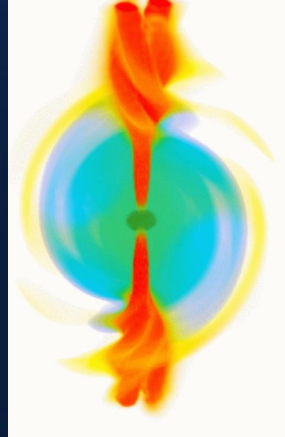
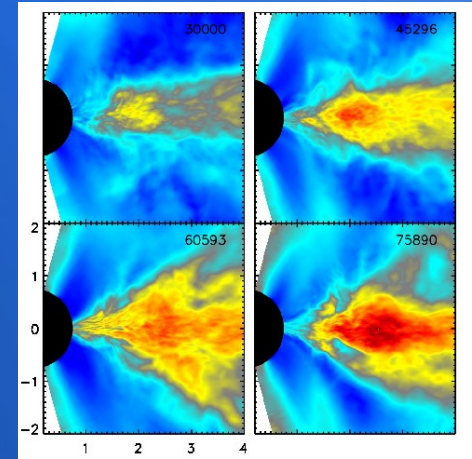
MacFadyen
et al 2008



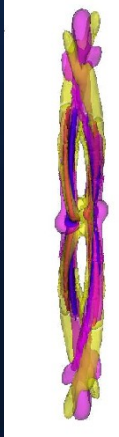
Shi et al 2011



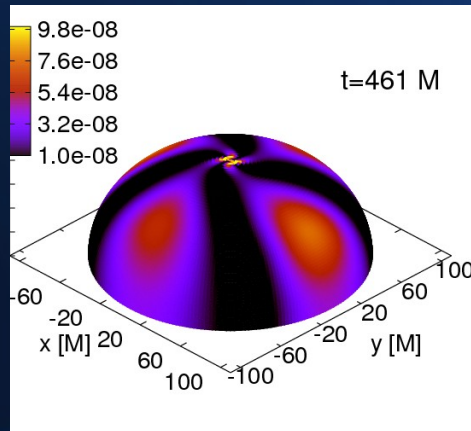
Noble et al 2012



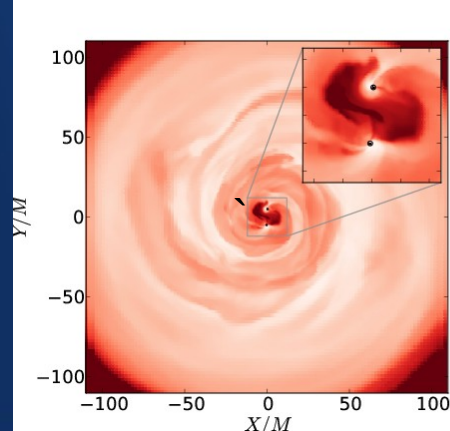
Palenzuela
et al 2010



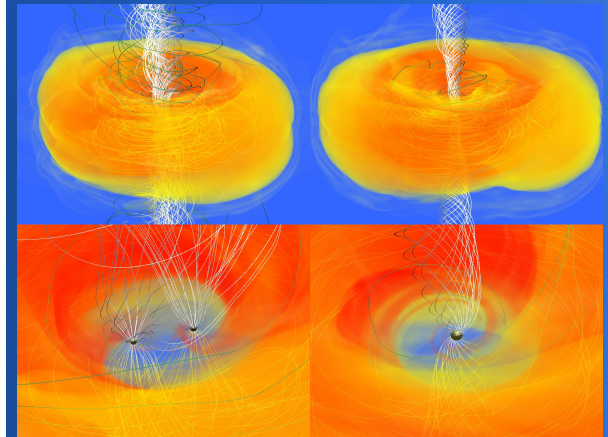
Alic
et al 2012



Moesta et al 2012



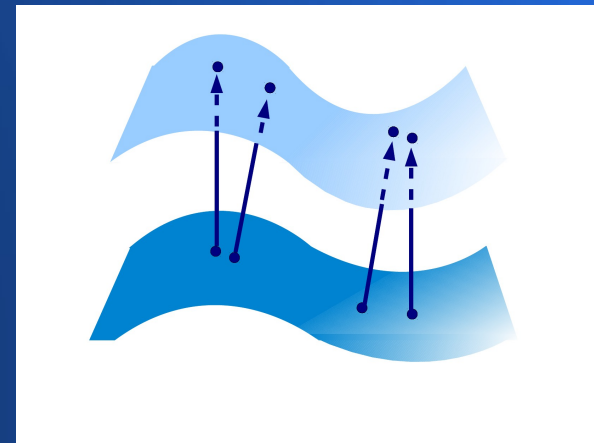
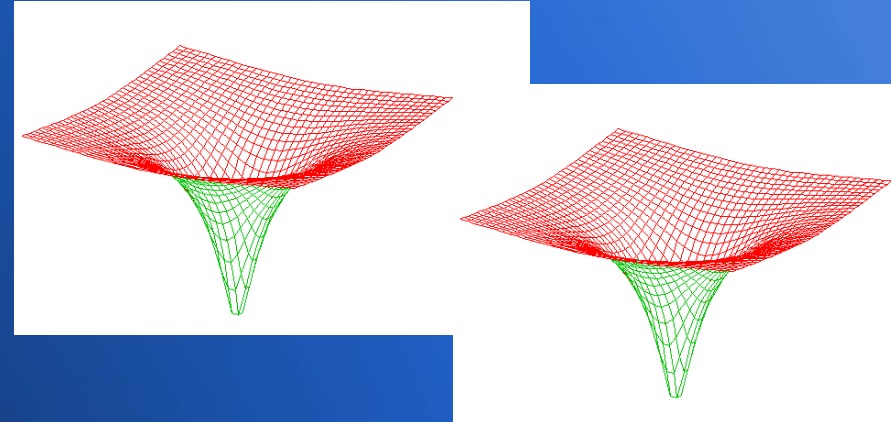
Farris et al 2012



Gold et al 2014

Methods (I): Numerical Relativity

- 3+1 split (foliate spacetime)
- Initial data:
Conformal-Thin-Sandwich Formalism
 - quasi-equilibrium data
 - helical Killing vector
- Predecoupling:
Analytically rotate CTS metric ID
- Postdecoupling:
BSSN formulation
“**moving punctures**” gauge conditions
 - system is strongly hyperbolic
 - Vacuum Cauchy Problem is well-posed
 - Slices penetrate horizons
 - Singularities at origin can be handled



Methods (II): ideal GRMHD

Illinois GRMHD AMR code

- Perfect fluid stress energy tensor

$$T^{\mu\nu} = (\rho_0 h + b^2) u^\mu u^\nu + \left(P + \frac{b^2}{2} \right) g^{\mu\nu} - b^\mu b^\nu$$

- Eom: Conservation laws (incl. cooling)

$$\nabla_\alpha (T^{\alpha\beta} + R^{\alpha\beta}) = 0$$

$$\nabla_\mu (\rho_0 u^\mu) = 0$$

- Induction equation for A-field

$$\partial_t A_i = \tilde{\epsilon}_{ijk} v^j \tilde{B}^k - \partial_i (\alpha \Phi - \beta^j A_j)$$

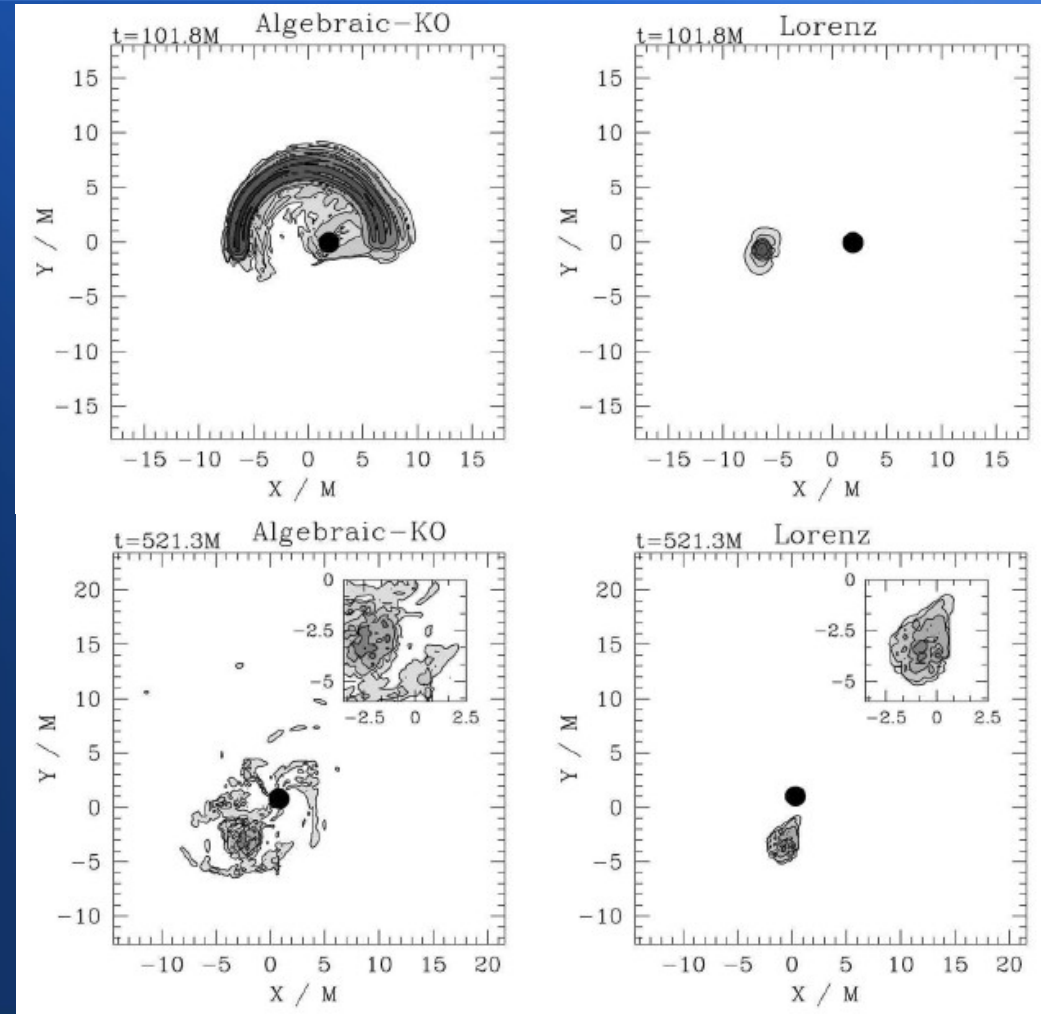
- Generalized Lorenz gauge condition

$$\nabla_\mu \mathcal{A}^\mu = \xi n_\mu \mathcal{A}^\mu$$

$$\mathcal{A}_\mu = \Phi n_\mu + A_\mu$$

Methods III: Generalized Lorenz gauge

- Previously used gauge conditions have zero speed modes
- Lorenz gauge modes propagate at c^*
- Generalized Lorenz gauge **damps gauge modes to zero** *
→ * Reduce spurious generation of B-field near AMR boundaries
- **Crucial** for long-term simulations



Method (III): Artificial Cooling

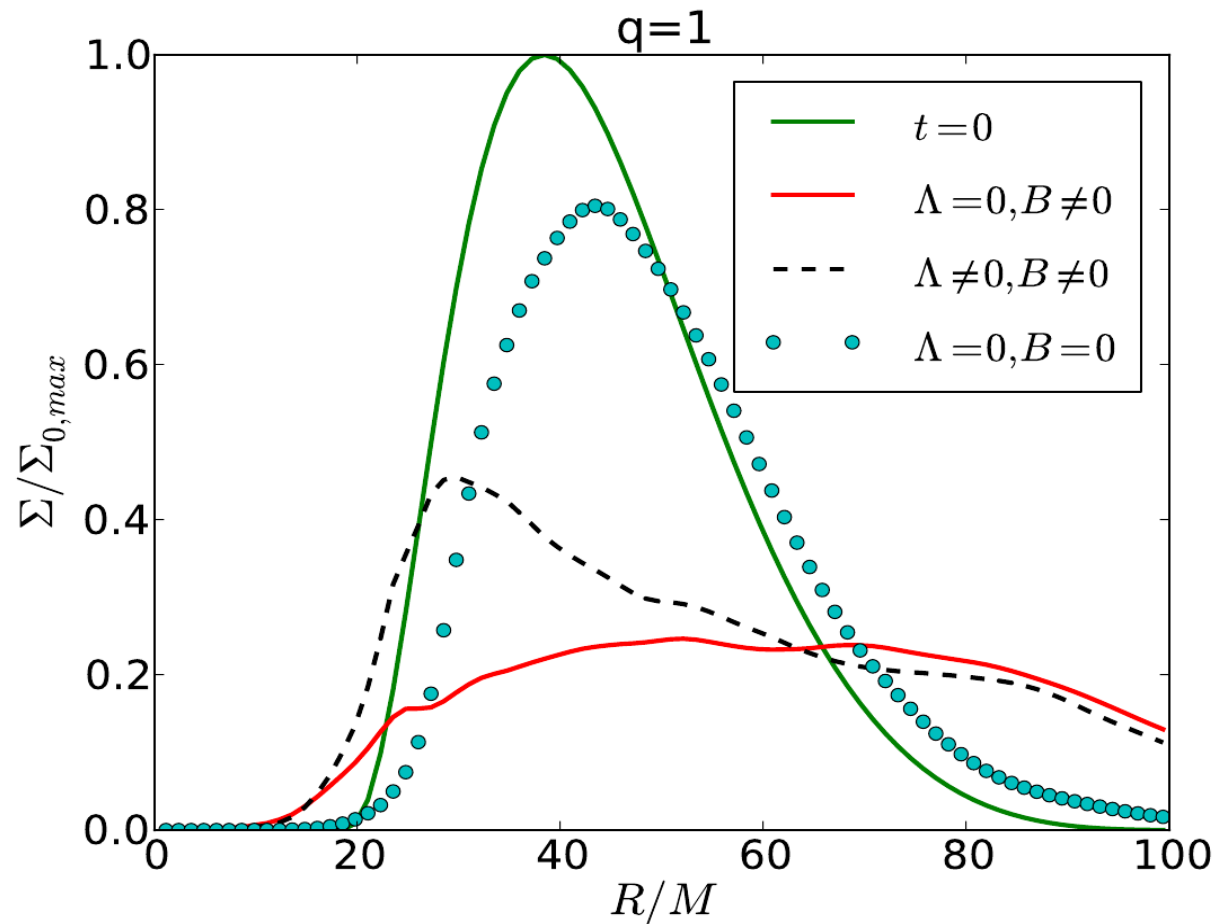
- Realistic cooling depends on detailed microphysics
 - Consider two extreme opposite limiting cases
 - (I) no-cooling
 - (II) radiate away all shock generated entropy on a local Keplerian time scale

$$\nabla_\nu T_{MHD}^{\mu\nu} = -\nabla_\nu T_{RAD}^{\mu\nu} = -\Lambda u^\mu$$

Λ : remove any (shock-)generated entropy

- Bracket real situation by two limiting cases
EOS: Ideal Gamma-law

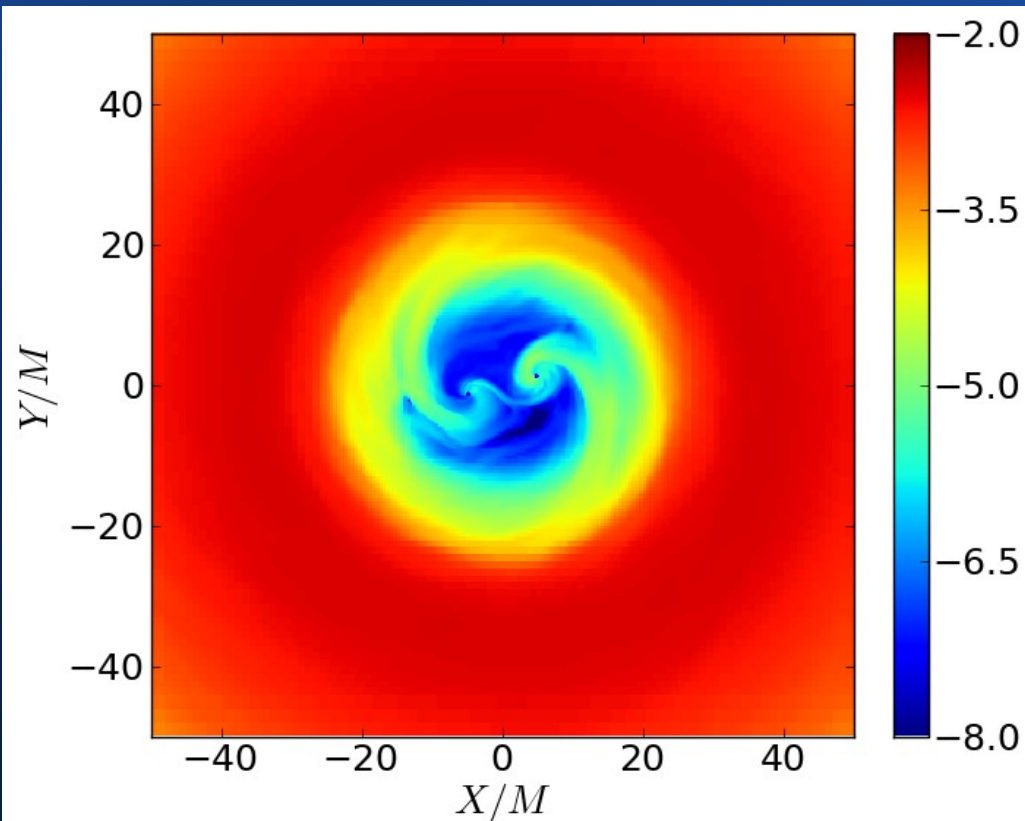
Surface density profiles



RESULTS

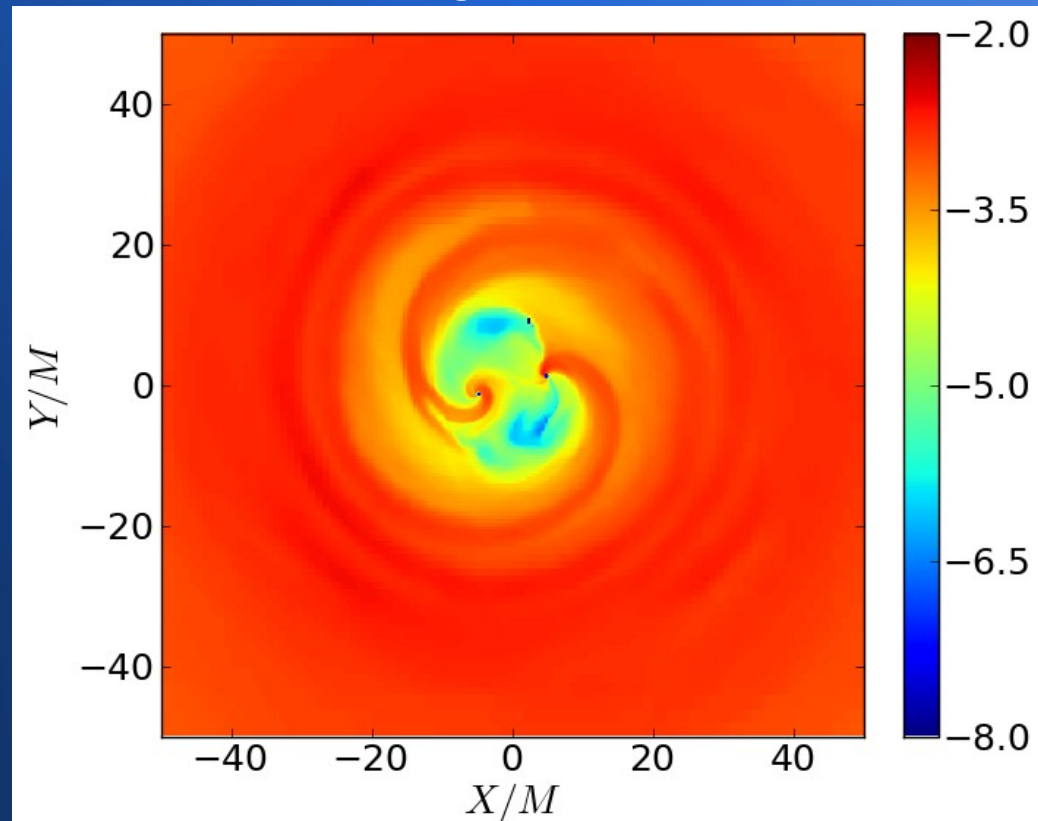
Importance of magnetic fields

Pure hydro



→ accretion / luminosities underestimated by orders of magnitude!

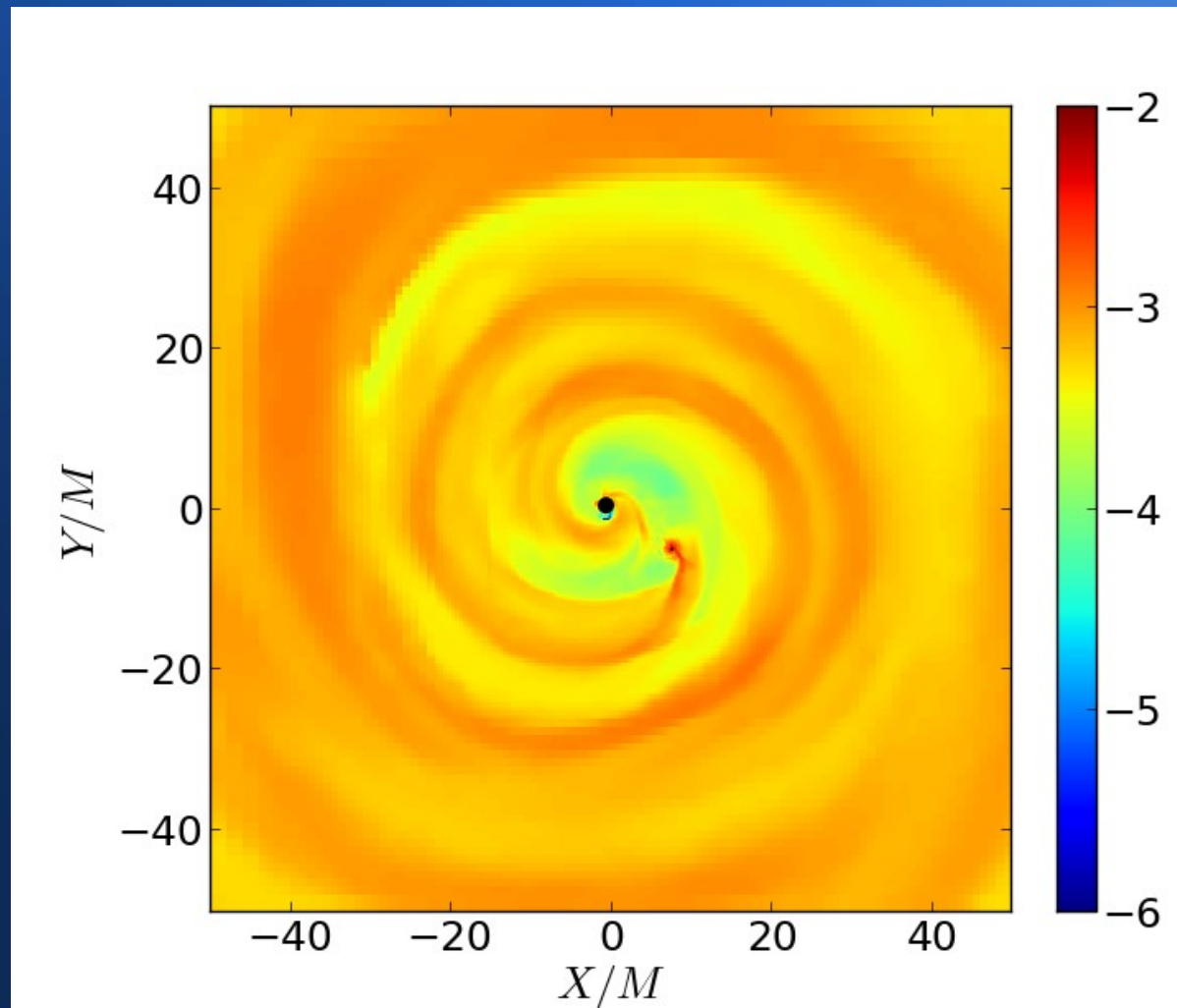
Magnetized



→ **can't ignore magnetic fields!**

1:10 (no-cooling)

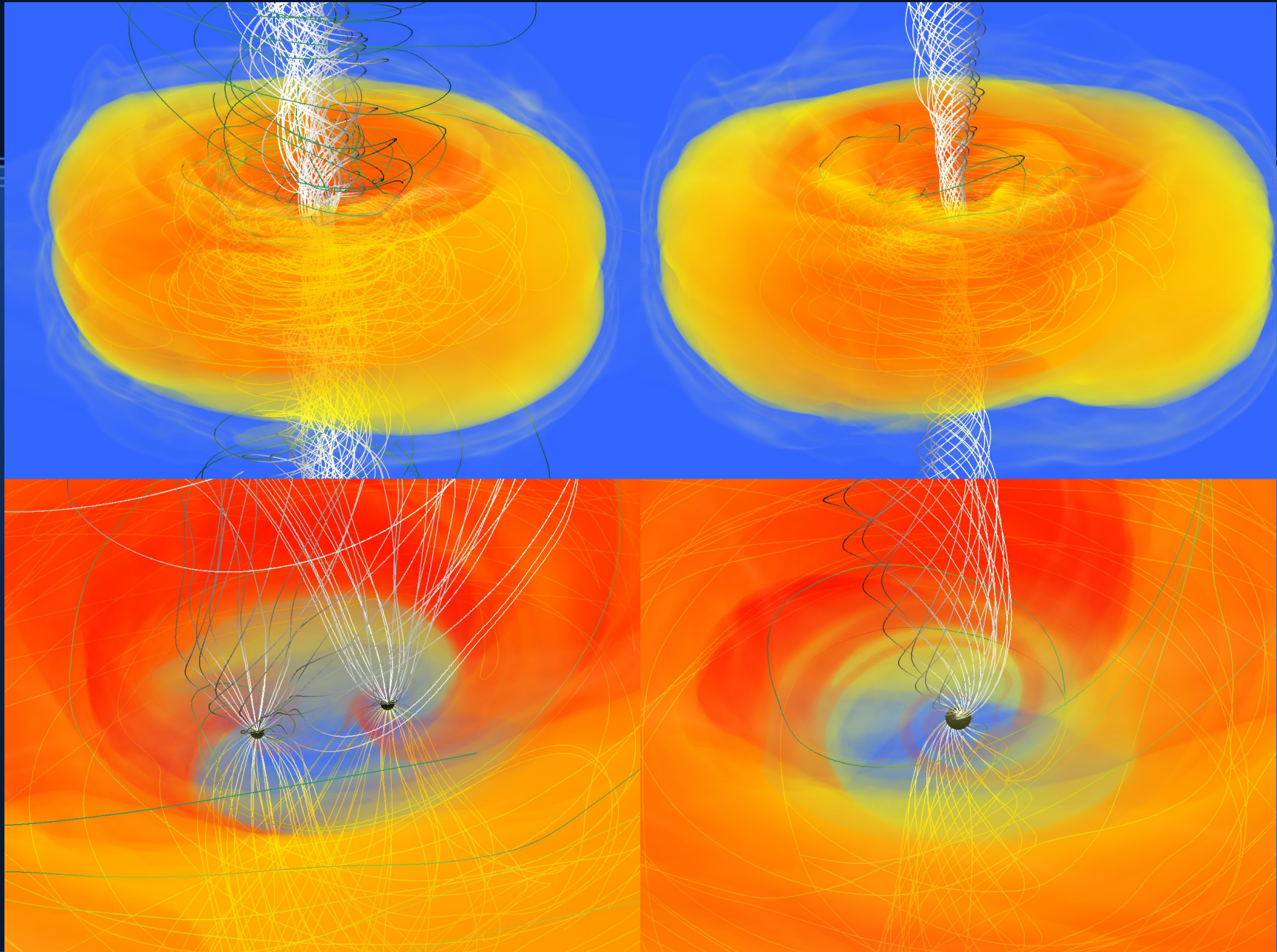
- Refilling of gap/cavity
- Binary fully emerged in highly magnetized gas
- Densest gas is near the (smaller) horizon



predecoupling

Just after merger

Total view
Zoom-in view



Outflows

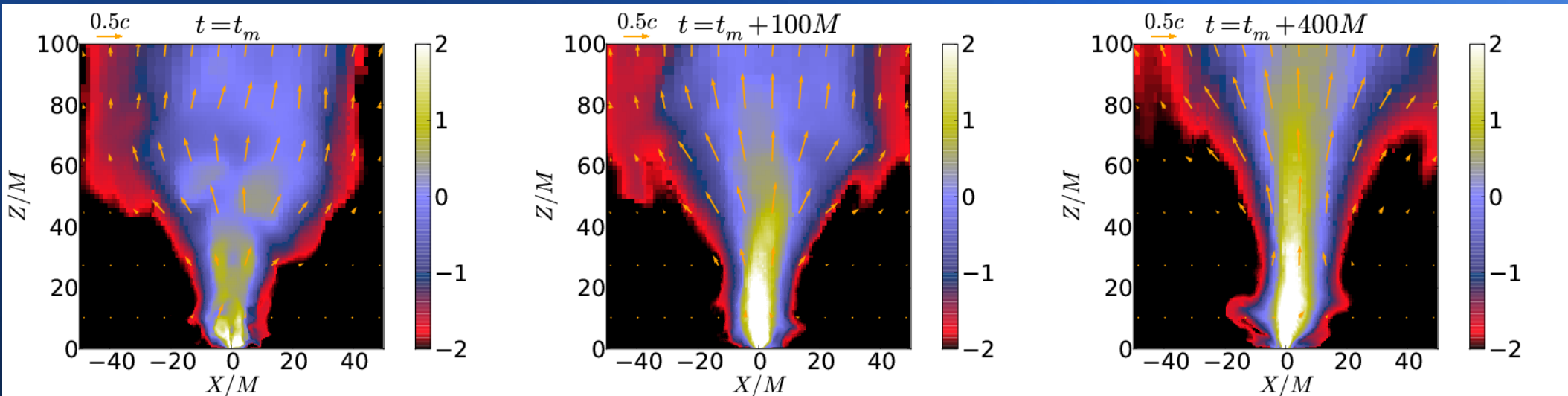
Density (log scale)

Magnetic pressure/
Density (log scale)



→ highly magnetized, relativistic outflows

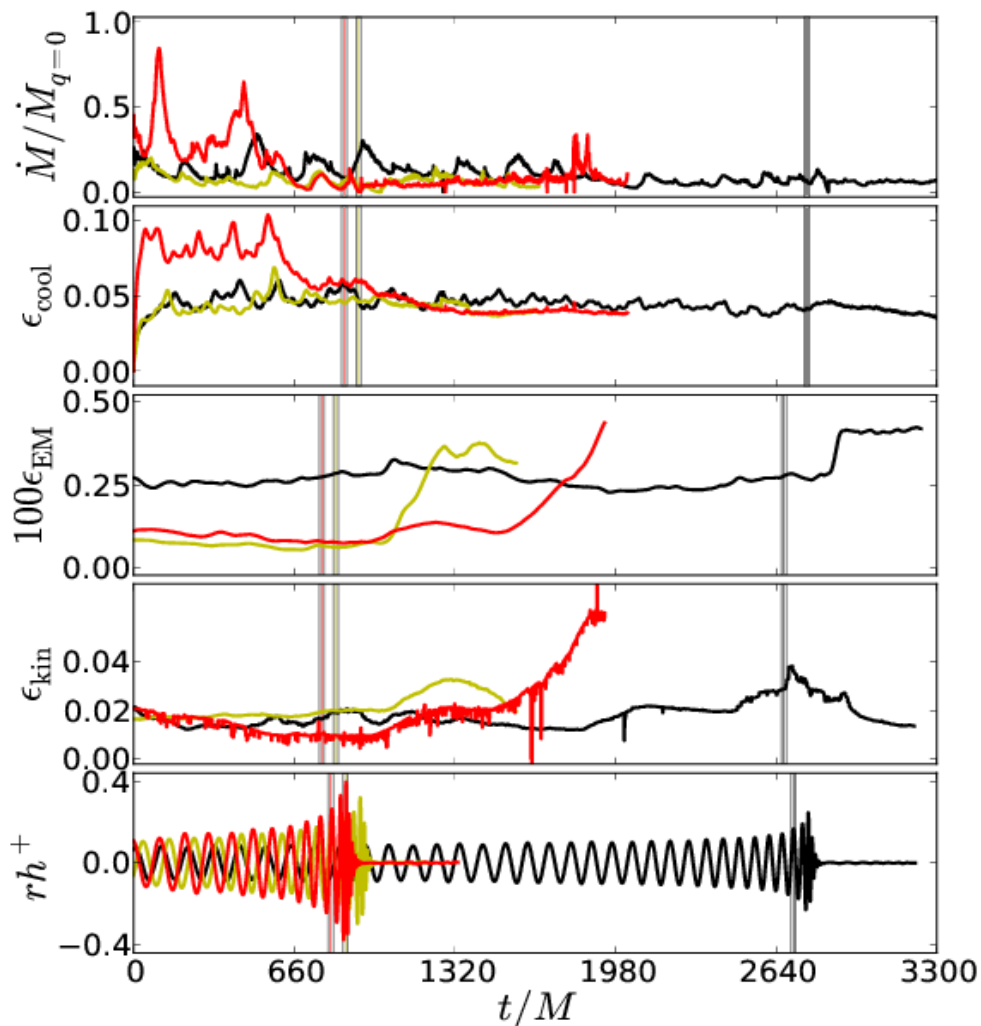
Transient jet feature around merger



AFTER MERGER:

- Enhanced collimation
- Increase in magnetic energy in outflows
- Speed up of outflow

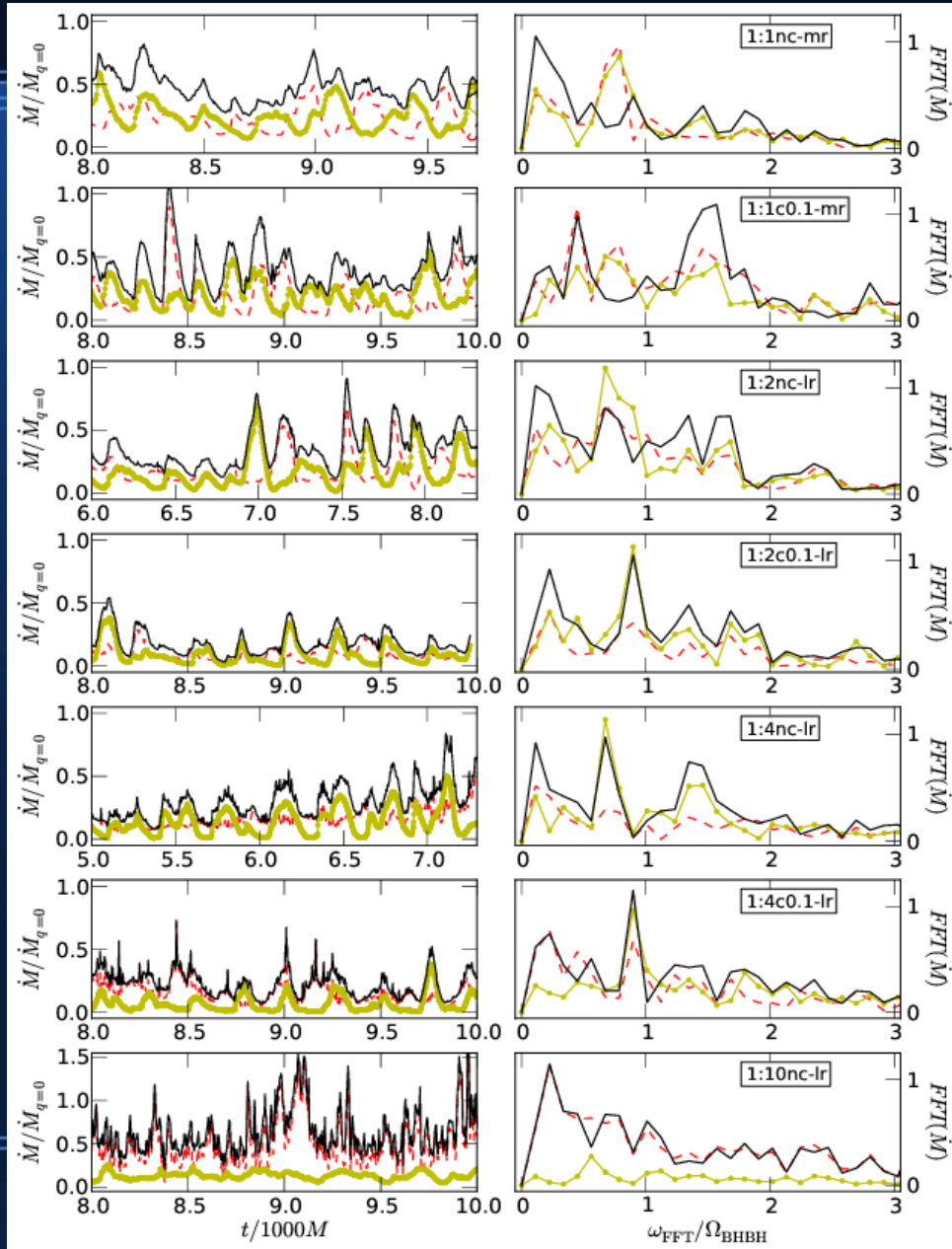
Accretion rates / Luminosities



Colors: Binary mass-ratio 1:1, 1:2, 1:4

- **Mass accretion rates:**
comparable to single BH case
- **Cooling luminosity:**
not sensitive to mass ratio
(except 1:1 predecoupling)
- **EM+KIN Luminosities:**
Characteristic rises/peaks
just after merger
 $L_{\text{cool}} > L_{\text{kin}} > L_{\text{EM}}$
- **GW amplitude:**
well known chirp

Variability



- far from clean (compare to 2D-thin disk studies)
- Not necessarily at binary orbital period
- Highest variability at intermediate mas ratios (confirming d'Orazio, Haiman et al)
- Little variability at larger mass ratios (as expected: $\rightarrow$ single BH limit)

Conclusions

- ✓ Predecoupling:

Gold et. al. 2013

high accretion rates, dense material remains near horizons, persistent jets

- ✓ inspiraling and merger:

Farris et al 2012
Gold et. al. 2014

Luminosity peaks/rises, enhanced jet collimation

- ✓ First GRMHD parameter study:

Gold et. al. 2013

binary mass ratio, e.g. 1:10 cavity refills

→ ***Now: Time for more physics !***

The next steps...

- × Radiative transport (synchrotron, Compton)
...in progress...
- × Rebrightening (viscous refilling of the hollow)
...in progress...
- × BH spins
...in progress...

Thank you for your attention!

References:

arXiv:1410.1543, PRD 90, 10, 104030

arXiv:1312.0600, PRD 89, 6, 064060

arXiv:1207.3354, PRL 109, 221102